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An improved global analysis of nuclear parton distribution functions including RHIC data

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ABSTRACT: We present an improved leading-order global DGLAP analysis of nuclear parton distribution functions (nPDFs), supplementing the traditionally used data from deep inelastic lepton-nucleus scattering and Drell-Yan dilepton production in proton-nucleus collisions, with inclusive high- p_T hadron production data measured at RHIC in d+Au collisions. With the help of an extended definition of the χ^2 function, we now can more efficiently exploit the constraints the different data sets offer, for gluon shadowing in particular, and account for the overall data normalization uncertainties during the automated χ^2 minimization. The very good simultaneous fit to the nuclear hard process data used demonstrates the feasibility of a universal set of nPDFs, but also limitations become visible. The high- p_T forward-rapidity hadron data of BRAHMS add a new crucial constraint into the analysis by offering a direct probe for the nuclear gluon distributions — a sector in the nPDFs which has traditionally been very badly constrained. We obtain a strikingly stronger gluon shadowing than what has been estimated in previous global analyses. The obtained nPDFs are released as a parametrization called EPS08.

KEYWORDS: Deep Inelastic Scattering, Hadronic Colliders, Parton Model, QCD.

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1. Introduction

With collider energies presently reached at BNL-RHIC, hard processes have become more and more important as diagnostic tools in the phenomenology of heavy ion collisions, QCD matter and QCD dynamics. The soon starting LHC heavy-ion program will emphasize the role of hard processes even further, by extending the kinematical range probed in the longitudinal momentum fraction x and in the process virtuality scale Q^2 by several orders of magnitude with respect to the presently accessible ones. The existence of well-constrained up-to-date nuclear parton distribution functions (nPDFs) will thus be essential for the correct interpretation of the data.

Sets of collinearly factorized universal nPDFs, which are obtained in global perturbative QCD analyses paralleling those for the free proton, are available [1-7], see also ref. [8]. These nPDFs are typically obtained by first parametrizing the nuclear corrections for each parton flavour relative to a known set of the free proton PDFs, and imposing constraints from sum rules at a chosen initial scale Q_0^2 . A best fit to nuclear hard-process data from deep inelastic lepton-nucleus scattering (DIS) and the Drell-Yan (DY) process in proton-nucleus collisions is obtained by an iterative procedure which involves the DGLAP evolution [9] of the (absolute) nPDFs. The best global fit then fixes the initial nuclear corrections.

Since the first of the nPDF sets, EKS98 [1, 2], the procedure has been improved by performing the analysis at next-to-leading order (NLO) [6, 7] and by making uncertainty

estimates [3, 5, 7] in analogy with the free proton case. In spite of such important progress, however, new data sets of relevance, which would more directly constrain the nuclear gluons in particular, have not been included in these ten years. The purpose of this paper is to make progress precisely in this respect, by including the data from inclusive high- p_T hadron production in d+Au collisions at RHIC in the global analysis of the nPDFs for the first time.

The most serious difficulty in the global DGLAP analyses of nPDFs has traditionally been the lack of experimental data which would impose stringent enough constraints for the nuclear gluon distributions. The extraction of the nPDFs would be cleanest in DIS but basically no high-precision data are at hand in the perturbative region $Q^2 \gtrsim 1 \text{ GeV}^2$ at $x \lesssim 0.01$ there. This deficiency translates into a bad determination of the nPDFs, gluons in particular, in a region, where the nuclear effects are sizeable and which will be frequently accessed at the LHC. For the analysis of hard processes taking place at midrapidities at RHIC the situation has been better, as the available DIS and DY data constrain the nPDFs in most of the kinematic range probed. In the forward-rapidity domain, however, the hard processes are sensitive to nPDFs at smaller values of x than what is presently constrained by DIS and DY: These RHIC data offer a possibility for independent further constraints of the nuclear gluon sector in the global analysis.

As discussed in previous works, [3, 10], the suppression in high- p_T hadron production at forward rapidities in d+Au collisions relative to p+p collisions, measured by BRAHMS [11], would seem to suggest stronger gluon shadowing than, e.g., in the EKS98 set. This suppression has been also proposed as a signal of parton saturation being reached at RHIC [12], so that the compatibility of the measured suppression with DIS and DY data sets within the DGLAP framework is a question of special relevance from the QCD parton dynamics point of view as well.

In this paper, we shall demonstrate for the first time, that a global fit of a very good quality can indeed be obtained by simultaneously accommodating the DIS, DY and high- p_T RHIC data in the leading-order (LO) DGLAP framework, i.e. that a relevant new set of universal, process-independent, collinearly factorized nPDFs can indeed be extracted, and that the gluon shadowing obtained at the smallest values of x is indeed stronger than in previous global fits. Also limitations and uncertainties remaining in the analysis are discussed in light of the results obtained. An important new feature which we introduce in the global χ^2 -analysis here — borrowing it from the free proton analyses [13] — is the treatment of data normalization errors given by the RHIC experiments. In particular, we demonstrate that only by accounting for these systematic errors, a meaningful comparison with the RHIC high- p_T pion data [14–16] can be done.

Parametrizing the obtained nuclear effects for each parton flavour in x, Q^2 and A and making a simple fast computer code available for public use has proven to be a working idea in the past. Analogously with our previous EKS98 set [1, 2], we now release a new set of nPDFS called EPS08, which is available at [17].

The rest of this paper is organized as follows: In section 2 we present the framework and analysis method, introducing the functional forms used and, in particular, the improvements in the χ^2 fitting procedure. In section 3 we present the results from the global fit, the new set of nPDFs, and the comparison with experimental data. The effects of the normalization-error treatment are demonstrated. In section 4 we comment on the strong gluon shadowing solution found. Conclusions and outlook are presented in section 5.

2. Framework and analysis method

2.1 Definition of nPDFs

The DGLAP framework we use is essentially the same as in our previous global fits of nPDFs [1-3]. For each parton flavour *i*, we define the nPDFs $f_i^A(x, Q^2)$ as the PDFs of protons bound to a nucleus of mass number A,

$$f_i^A(x,Q^2) \equiv R_i^A(x,Q^2) f_i^{\text{CTEQ6L1}}(x,Q^2),$$
(2.1)

where $f_i^{\text{CTEQ6L1}}(x, Q^2)$ is obtained from the latest LO CTEQ set of the free proton PDFs [18], and $R_i^A(x, Q^2)$ is the nuclear modification factor for this parton flavour. We also assume that PDFs of bound neutrons can be obtained on the basis of isospin symmetry. For instance, the total u quark PDF in a nucleus A with Z protons then becomes

$$u_A(x,Q^2) = Zf_u^A(x,Q^2) + (A-Z)f_d^A(x,Q^2).$$

The nuclear effects of Deuterium (A = 2) and those in the cumulative region x > 1 are neglected. We do not discuss the dependence of the nPDFs on transverse location inside the nucleus (the impact parameter dependence) [10, 19] here, either, only the average nuclear effects are considered.

We parametrize the nuclear modifications R_i^A at an initial scale $Q_0^2 = 1.69 \,\text{GeV}^2$, which conveniently matches the lowest scale and the charm-quark mass threshold in the CTEQ6L1 set. The valence quark modifications are constrained by baryon number conservation and the gluon modifications by momentum conservation. At higher scales $Q^2 > Q_0^2$ the nPDFs are then obtained by solving the conventional DGLAP equations [9] at LO numerically, applying the fast solution method introduced in [20].

In order to reduce the amount of fitting parameters, and obtain a converging wellconstrained fit, we have to assume initially flavour-independent nuclear effects for valence quarks, sea quarks and gluons, i.e. we parametrize only three different functions: $R_V^A(x, Q_0^2)$ for all valence quarks, $R_S^A(x, Q_0^2)$ for all sea quarks, and $R_G^A(x, Q_0^2)$ for gluons. In the DGLAP evolution, each flavour is considered individually so that at $Q^2 > Q_0^2$ the modifications may in principle depend on parton flavour.

2.2 Fitting functions and parameters

Choosing a suitable functional form for the input nuclear modification factors $R_i^A(x, Q_0^2)$ is among the most troublesome and crucial issues in the global nPDF analyses. On one hand the fit functions must be flexible enough, i.e. there should appear sufficiently many parameters so that all the relevant features suggested by the data can be caught. On the other hand, too large a number of parameters easily leads to badly converging fits. Thus



Figure 1: An illustration of the smoothly matched fit functions $R_i^A(x)$ and the role of the parameters x_a^A , y_a^A , x_e^A and Δ_e^A . The superscripts A have been suppressed in the figure.

the number of parameters always is a compromise between the flexibility of the fit and the feasibility of the χ^2 -analysis.

Up to now, gluon shadowing in the small-x region $x \leq 10^{-2}$ has been constrained only by the momentum sum rule, and it has been essentially dictated by the assumed form of the fit function. Also the statistical error bars computed then reflect the uncertainties within the fit function chosen. Thus, as discussed in [3], there has been a large uncontrolled error in the gluon shadowing. The inclusion of the high- p_T hadron data from RHIC at forward rapidities, however, now provides important further constraints for the gluon shadowing region, which will be exploited in the present work.

In order to take into account the RHIC high- p_T forward-rapidity hadron data, which suggest a stronger gluon shadowing than obtained in previous global analyses (see the discussion in [3]), we need to modify the parametrization of the shadowing region. In our past works, we assumed a saturation of the modifications $R_i^A(x, Q_0^2)$ such that $R_G^A \approx R_S^A \rightarrow$ const at $x \to 0$. This assumption is relaxed in the present analysis, and we introduce a power-law behaviour of the nuclear modification factors at small x as follows

$$R_i^A(x, Q_0^2) \stackrel{x \to 0}{\sim} x^{\alpha^A}, \qquad \alpha^A > 0.$$
 (2.2)

This can be motivated by the (approximate) power-law behaviour $\sim x^{-P_{\text{free}}}$ of the free proton PDFs at small-x, assuming that the nPDFs share this same gross feature but with a different power $P_{\text{free}} \geq P_{\text{bound}}$. This means that $R_i^A \sim x^{(P_{\text{free}} - P_{\text{bound}})} \to 0$ as $x \to 0$.

With this assumption as a guide, we parametrize the initial nuclear modifications R_V^A , R_S^A and R_G^A in three pieces as illustrated in figure 1: $R_1^A(x)$ at small values of x, below the antishadowing maximum, $x \le x_a^A$; $R_2^A(x)$ from the antishadowing maximum to the EMC minimum, $x_a^A \le x \le x_e^A$; and $R_3^A(x)$ in the large-x Fermi-motion region, $x \ge x_e^A$;

$$R_1^A(x) = c_0^A + (c_1^A + c_2^A x^{\alpha^A}) [\exp(-x/x_s^A) - \exp(-x_a^A/x_s^A)], \ x \le x_a^A$$

$$R_2^A(x) = a_0^A + a_1^A x + a_2^A x^2 + a_3^A x^3, \qquad x_a^A \le x \le x_e^A$$

$$R_3^A(x) = \frac{b_0^A - b_1^A x}{(1-x)^{\beta^A}} + b_2^A (x - x_e)^2, \qquad x_e^A \le x \le 1.$$
(2.3)

Some of the parameters above are eliminated by matching the different pieces smoothly together: we require continuity of the fit functions and zero first-derivatives at the antishadowing maximum x_a^A and at the EMC minimum x_e^A . The required behavior (2.2) fixes c_0^A . It is convenient to express the fit functions in terms of the following 8 parameters,

 $\begin{array}{ll} \alpha^A & \mbox{the power according to which } R_1^A \to 0 \mbox{ at } x \to 0, \\ x_s^A & \mbox{a slope factor in the exponential,} \\ x_a^A, y_a^A & \mbox{position and height of the antishadowing maximum} \\ x_e^A, & \mbox{position of the EMC minimum} \\ \Delta_e^A & \mbox{difference of the antishadowing maximum and the EMC minimum} \\ \beta^A, b_2^A & \mbox{slope factors in the Fermi-motion part } R_3 \mbox{ at } x > x_e. \end{array}$

In principle, all parameters above are different from one nucleus to another, hence the superscript A. For the A dependence we assume a simple power law,

$$z_i^A = z_i^{A_{\rm ref}} \left(\frac{A}{A_{\rm ref}}\right)^{p_{z_i}},\tag{2.4}$$

where $z_i = x_s, x_a, y_a \dots$, and choose the reference nucleus to be Carbon, $A_{ref} = 12$.

With momentum and baryon number sum rules, we can fix α^A for gluons and valence quarks, and thus reduce the total number of parameters to 44. This is still far too many for a convergent χ^2 -minimization with the nuclear data constraints available. To proceed, additional assumptions need to be introduced — how the unconstrained regions of the phase space are handled, and how the number of final fit parameters is reduced down to 15 by fixing those parameters which cannot be constrained, is explained in section 3.1.

2.3 Data sets

The experimental data, providing the nonperturbative input for the nPDFs, in our present analysis covers three types of hard processes involving nuclei: In addition to the data from lepton-nucleus deep inelastic scattering and proton-nucleus Drell-Yan dilepton production, as a new ingredient we include the data from inclusive high- p_T hadron production in minimum-bias d+Au collisions from the BRAHMS, PHENIX and STAR collaborations at RHIC. In total, we have over 600 data points covering 13 nuclei from Helium up to Lead. Table 1 summarizes the data sets in our analysis.

The (minimum bias) DIS and DY data that we utilize are available as ratios of differential cross sections between a nucleus A and a reference nucleus. We denote the cross section ratios computed against deuterium as

$$R_{\rm DIS}^{\rm A}(x,Q^2) \equiv \frac{\frac{1}{A} d\sigma_{\rm DIS}^{l\rm A}/dQ^2 dx}{\frac{1}{2} d\sigma_{\rm DIS}^{\rm ld}/dQ^2 dx} \stackrel{\rm LO}{=} R_{F_2}^{\rm A}(x,Q^2), \qquad R_{\rm DY}^{\rm A}(x,M^2) \equiv \frac{\frac{1}{A} d\sigma_{\rm DY}^{\rm p\rm A}/dM^2 dx}{\frac{1}{2} d\sigma_{\rm DY}^{\rm p\rm d}/dM^2 dx},$$
(2.5)

where x refers to the momentum fraction and Q^2 to the photon virtuality for DIS, and M^2 to the invariant mass of the lepton pair and x to either x_1 or x_2 for DY. The scales Q^2 and M^2 also define our factorization scales, and we consider only those data points which lie above our initial scale: $M^2, Q^2 > 1.69 \,\text{GeV}^2$.

Experiment	Process	Nuclei	Data points	χ^2	Weight	Ref.
SLAC E-139	DIS	He(4)/D	18	2.0	1	[25]
NMC 95, reanalysis	DIS	He/D	16	12.1	1	[26]
NMC 95	DIS	Li(6)/D	15	30.7	1	[27]
SLAC E-139	DIS	Be(9)/D	17	5.5	1	[25]
NMC 96	DIS	$\mathrm{Be}(9)/\mathrm{C}$	15	4.2	1	[28]
SLAC E-139	DIS	C(12)/D	7	3.5	1	[25]
NMC 95	DIS	C/D	15	10.5	5	[27]
NMC 95, reanalysis	DIS	C/D	16	17.8	5	[26]
NMC 95, reanalysis	DIS	C/Li	20	36.4	1	[26]
FNAL-E772	DY	C/D	9	8.9	10	[29]
SLAC E-139	DIS	Al(27)/D	17	3.6	1	[25]
NMC 96	DIS	Al/C	15	6.7	1	[28]
SLAC E-139	DIS	Ca(40)/D	7	1.3	1	[25]
FNAL-E772	DY	Ca/D	9	5.0	10	[29]
NMC 95, reanalysis	DIS	Ca/D	15	27.9	1	[26]
NMC 95, reanalysis	DIS	Ca/Li	20	26.1	1	[26]
NMC 96	DIS	Ca/C	15	6.3	1	[28]
SLAC E-139	DIS	Fe(56)/D	23	16.5	1	[25]
FNAL-E772	DY	$\rm Fe/D$	9	5.0	10	[29]
NMC 96	DIS	$\rm Fe/C$	15	11.9	1	[28]
FNAL-E866	DY	Fe/Be	28	21.6	1	[30]
CERN EMC	DIS	Cu(64)/D	19	12.3	1	[31]
SLAC E-139	DIS	Ag(108)/D	7	2.3	1	[25]
NMC 96	DIS	Sn(117)/C	15	10.9	1	[28]
NMC 96, Q^2 dep. $x \le 0.025$	DIS	$\mathrm{Sn/C}$	24	9.4	10	[32]
NMC 96, Q^2 dep. $x > 0.025$	DIS	$\mathrm{Sn/C}$	120	75.2	1	[32]
FNAL-E772	DY	W(184)/D	9	10.0	10	[29]
FNAL-E866	DY	W/Be	28	26.5	1	[30]
SLAC E-139	DIS	Au(197)/D	18	6.1	1	[25]
RHIC-BRAHMS	h^- prod.	dAu/pp	6	2.2	40	[11]
RHIC-PHENIX	π^0 prod.	dAu/pp	35	21.3	1	[14, 15]
RHIC-STAR	$\pi^+ + \pi^-$ prod.	dAu/pp	10	3.5	1	[16]
NMC 96	DIS	Pb/C	15	5.1	1	[28]
total			627	448		

Table 1: The data used in this analysis. The mass numbers are indicated in parentheses and the number of data points refers to those falling within our kinematical cuts, $Q^2, M^2 \ge 1.69 \text{ GeV}^2$ for DIS and DY, and $p_T \ge 2 \text{ GeV}$ for hadron production at RHIC. The quoted χ^2 values correspond to the unweighted contributions of each data set.

The inclusive hadron production data at RHIC comes as the nuclear modification factor R_{dAu} , the ratio between the invariant yields in d+Au and p+p collisions,

$$R_{\rm dAu} = \frac{1}{\langle N_{\rm coll} \rangle} \frac{d^2 N^{\rm dAu}/dp_T d\eta}{d^2 N^{\rm pp}/dp_T d\eta} \stackrel{\rm min, bias}{=} \frac{\frac{1}{2A} d^2 \sigma^{\rm dAu}/dp_T d\eta}{d^2 \sigma^{\rm pp}/dp_T d\eta},$$
(2.6)

where p_T and η denote the transverse momentum and the pseudorapidity of the observed hadron, and $\langle N_{\text{coll}} \rangle$ is the estimated average number of inelastic binary nucleon-nucleon collisions in a centrality class studied. The last equality holds for the minimum bias case which we are interested in here. According to the QCD factorization theorem, the inclusive hadron production cross sections can be computed as

$$d\sigma^{AB \to h+X} = \sum_{ijkl} f_i^A(Q^2) \otimes f_j^B(Q^2) \otimes \sigma^{ij \to kl}(Q^2) \otimes D_{k \to h+X}(Q_f^2), \tag{2.7}$$

where $f_i^A(Q^2)$ are the input nPDFs, $\sigma^{ij \to kl}(Q^2)$ is the pQCD matrix element squared, and $D_{k \to h+X}(Q_f^2)$ denotes the fragmentation functions for which we use the KKP parametrization [21]. Our choice for the fragmentation scale is the hadronic transverse momentum, $Q_f^2 = p_T^2$, and for the factorization and renormalization scale Q^2 we take the corresponding partonic transverse momentum. Notice here that all the scale choices above are simplifications in the sense that they could be left as additional fit parameters, and that the KKP fragmentation functions do not distinguish negatively and positively charged hadrons. Such details, however, are beyond the scope of the present analysis. A more detailed discussion of how the needed differential cross sections (2.7) are calculated in practice in LO can be found in [22].

We should emphasize that the following choices are made with the inclusion of the RHIC data:

- Since we do not discuss the impact parameter dependent nuclear effects here, we consider only minimum bias data for R_{dAu} .
- From PHENIX and STAR, we systematically include only the pion production data. This is because the 'Cronin-type' enhancement seems to be much larger for baryons than for mesons [14], signalling of the fact that still at $\sqrt{s_{\rm NN}} = 200 \,{\rm GeV}$ there might be a significant component of nonperturbative baryon-number transport from the beam particles. We do, however, include the BRAHMS data for negatively charged hadrons with the assumption that the antiproton content in this data sample is negligible.
- Perturbative QCD calculations of inclusive hadron production, which are performed strictly in the framework of collinear factorization (without any intrinsic transverse momentum), show similar features both in LO [22] and in NLO [23, 24]: Below $p_T \sim$ a few GeV the computed cross sections for $p + p(\overline{p})$ collisions start to overshoot the data. Hence, since we should not push the nuclear case too far either, we choose to include only the region $p_T \geq 2$ GeV of the RHIC data on inclusive hadron production in this analysis. More discussion on this choice will follow later.

2.4 Modified χ^2

The established way of fitting a set of parameters $\{z\}$ of the PDFs against a large number of experimental data, is the minimization of the global χ^2 function. In its simplest form the global χ^2 , the goodness parameter of the fit obtained, is defined by

$$\chi^{2}(\{z\}) \equiv \sum_{N} \chi^{2}_{N}(\{z\}), \qquad (2.8)$$

where N labels the experimental data sets, and

$$\chi_N^2(\{z\}) \equiv \sum_{i \in N} \left[\frac{D_i - T_i(\{z\})}{\sigma_i} \right]^2,$$
(2.9)

where D_i , σ_i , and $T_i(\{z\})$ denote the value of a single data point, its measurement uncertainty, and the corresponding theoretical value which depends on the parameters $\{z\}$ of PDFs.

For the nPDF analyses involving only DIS and DY data, the simple form of χ^2 above has been sufficient, but for our current purposes a more general definition for the χ^2 , introduced in [13], is needed:

$$\chi^{2}(\{z\}) \equiv \sum_{N} w_{N} \chi^{2}_{N}(\{z\})$$
(2.10)

$$\chi_{N}^{2}(\{z\}) \equiv \left(\frac{1-f_{N}}{\sigma_{N}^{\text{norm}}}\right)^{2} + \sum_{i \in N} \left[\frac{f_{N}D_{i} - T_{i}(\{z\})}{\sigma_{i}}\right]^{2}, \qquad (2.11)$$

where w_N is a weight factor chosen separately for each data set, σ_N^{norm} is the relative uncertainty in the overall normalization reported by the experiment, and f_N is the optimized value of the overall normalization for the data set, corresponding to each parameter set $\{z\}$. The reasons for the necessity of such redefinition are the following:

- 1. By making the weight factor w_N larger than 1, we can emphasize by hand the importance of those data sets which contain definite physics content — such as constraints for small-x gluons — but whose number of data points is small. With a default value $w_N = 1$, such data sets would have a negligible contribution to the overall χ^2 and the valuable constraints they offer would escape unnoticed.
- 2. In addition to the point-to-point statistical and systematic errors, certain data sets have a significant common normalization uncertainty σ_N^{norm} for all data points within the set. Even if this normalization uncertainty is large, the *shape* of the distribution formed by the data points may be a valuable constraint for the nPDFs. We introduce for each data set a normalization factor $f_N \in [1 - \sigma_N^{\text{norm}}, 1 + \sigma_N^{\text{norm}}]$ which multiplies all the experimental values within the set N. In connection with f_N , there is an additional "penalty" factor $(\frac{1-f_N}{\sigma_N^{\text{norm}}})^2$ which is the larger the more f_N deviates from unity — this accounts for the fact that having $f_N = 1$ is anyway the experiment's best estimate for normalization. The actual value for f_N is determined from the requirement that $\chi_N^2(\{z\})$ for each data set is at minimum.

The motivation for both modifications in the χ^2 definition discussed above comes mainly from adding the RHIC data for the nuclear modification factor R_{dAu} of eq. (2.6) into the analysis. First, the BRAHMS data set for forward direction ($\eta \sim 2...3$, especially with our choice $p_T \geq 2 \text{ GeV}$) has only a very few data points. These would not have much effect in the global χ^2 without being artificially emphasized. Second, the average number of inelastic binary nucleon-nucleon collisions $\langle N_{coll} \rangle$ in d + Au collision is derived from a simulation of the experiment with the Glauber model as an input, which gives rise to a significant model-dependent normalization uncertainty in R_{dAu} .

The amount of DIS data overwhelms that of the DY data. To improve upon this balance, we weight the FNAL-E772 DY data set by $w_N = 10$. This improves the determination of the relative importance between the valence and sea quarks at intermediate values of x. For the NMC data set for $R_{F_2}^C$ we give a weight $w_N = 5$ in order to better ensure a good fit for the Carbon nucleus, which is used as reference in the analysis. The NMC 96 data on the Q^2 -dependence of $F_2^{\text{Sn}}/F_2^{\text{C}}$ is weighted by $w_N = 10$ but only for the three lowest values of x — the three upper panels in figure 8 below — to help constraining the gluon distribution at $x \leq 0.02$ via the DGLAP evolution. Finally, the few points of the BRAHMS data that we include in our analysis, are weighted by a large factor $w_N = 40$ in order to account for the constraints this data set gives for the gluon distribution. All these weights are summarized in table 1 above.

3. Results

3.1 Final parameters

In order to reach a well converging (well constrained) global fit, where none of the fit parameters are drifting to their limits, we are forced to reduce the total number of free parameters down to the following 15:

• Valence quark modification

The DIS data constrain the modification $R_V^A(x, Q_0^2)$ in the $x \gtrsim 0.1$ region rather well, and altogether 8 parameters x_a , y_a , p_{y_a} , x_e , Δ_e , p_{Δ_e} , b_2 , p_{b_2} were left free.

• Sea quark modification

The DIS and DY data probe the sea quarks in the region $0.01 \leq x \leq 0.1$, and 5 parameters, α , p_{α} , x_a , y_a , p_{y_a} , controlling this region in $R_S^A(x, Q_0^2)$, were left free. The region $x \geq 0.3$ is, however, not constrained by any present experimental data. We assume for simplicity a smooth behavior in this region, without an EMC effect.

• Gluon modification

The gluon modification $R_G^A(x, Q_0^2)$ at small x is now directly constrained by the inclusive hadron production data from RHIC. Indirectly the gluons are constrained by the Q^2 -evolution effects in the sea quark sector, reflected by the DIS and DY data. In spite of the new constraints, we were still able to leave only 2 parameters, y_a and p_{y_a} controlling the antishadowing peak height, free. We assume a similar EMC-effect for gluons as there is for valence quarks, guided by the shape of the preliminary PHENIX data for inclusive photon production in Au+Au collisions at $p_T \gtrsim 6 \text{ GeV}$ [33] and also by the PHENIX data for inclusive pion production at $\eta = 0$ and $p_T \gtrsim 6 \text{ GeV}$ [15] (see figure 12 ahead — we have checked that indeed some sensitivity to gluon PDFs persists even at these values of p_T).

The global fit with these 15 parameters was then performed by minimizing the χ^2 function defined in eqs. (2.10) and (2.11) with the MINUIT [34] routine from the CERN

Param.	Valence R_V^A	Sea R_S^A	Gluon R_G^A
α	α^A from baryon sum	$2.67 imes 10^{-2}$	α^A from momentum sum
p_{lpha}		$3.47 imes \mathbf{10^{-1}}$	
x_s	0.1, fixed	1.0, fixed	1.0, fixed
p_{x_s}	0, fixed	0, fixed	0, fixed
x_a	$7.37 imes10^{-2}$	0.580	0.15 fixed
p_{x_a}	0, fixed	0, fixed	0, fixed
x_e	0.751	as valence	as valence
p_{x_e}	0, fixed	0, fixed	0, fixed
y_a	1.04	0.997	1.13
p_{y_a}	$1.55 imes 10^{-2}$	-1.51 $ imes 10^{-2}$	$\boldsymbol{6.99}\ \times \boldsymbol{10^{-2}}$
Δ_e	0.138	0, fixed	from valence
p_{Δ_e}	0.257	0, fixed	from valence
b_2	13.3	0, fixed	0, fixed
p_{b_2}	0.278	0, fixed	0, fixed
eta	0.3, fixed	0.3, fixed	0.3, fixed
no	0 fixed	0. fixed	0. fixed

Table 2: List of all parameters defining the modifications R_V^A , R_S^A and R_G^A through eq. (2.3) at our initial scale $Q_0^2 = 1.69 \,\text{GeV}^2$. The parameters α , x_s , x_a , x_e , y_a , Δ_e , b_2 and β are for the reference nucleus A = 12, and the powers p_i define their A-dependence as in eq. (2.4). For valence quarks and gluons, the baryon number and momentum sum rules fix the parameters α^A for each nucleus A separately, in which case the powers p_{α} are not used. The location and height of the EMC minimum of R_G^A was fixed to that of R_V^A . The parameters left free for the minimization procedure are shown in bold face.

Program Library. Table 2 summarizes the parameter values obtained as well as the fixed parameters. The goodness of the fit is characterized by $\chi^2/N = 0.71$, where χ^2 is computed with no extra weights, $w_N = 1$, but with the optimized normalization factors f_N included, and N = 627 is the total number of data points. The contribution from each data set to this χ^2 can be read off from table 1. The corresponding nuclear modifications for selected nuclei at our initial scale $Q_0^2 = 1.69 \,\text{GeV}^2$ are shown in figure 2. Table 3 shows the contribution from different types of hard processes to the unweighted χ^2 and the comparison with our previous analysis in ref. [3]. The χ^2/N obtained in earlier global analyses can be found in table 3 of ref. [3].

3.2 Comparison with data

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The comparison of our results with the experimental data used in the global fit is presented in figures 3–8 for DIS, in figures 9–10 for DY, and in figures 11–12 for the RHIC data. In all figures, the open (red) symbols denote the experimental data. The error bars for the DIS and DY cases correspond to the point-to-point statistical and systematic errors added in quadrature, while for the RHIC data the statistical and systematic errors are shown separately.

Data type	Data points	$\chi^2_{ m EPS08}$	$\chi^2_{\rm EKPS}$
Deep Inelastic	484	344.2	337.4
Drell-Yan	92	77.1	84.3
Hadron production	51	26.9	28.0
Total	627	448.3	449.6

Table 3: Contributions of various data types to the total unweighted χ^2 in our previous work [3] (EKPS) and in this work (EPS08).



Figure 2: The nuclear modification factors R_V^A , R_S^A and R_G^A for C, Ca, Sn, and Pb at $Q_0^2 = 1.69 \text{ GeV}^2$. The DIS ratio $R_{F_2}^A$ is shown for comparison.



Figure 3: The computed ratio $R_{F_2}^A(x, Q^2)$ vs. $R_{F_2}^C(x, Q^2)$ compared with the NMC data [28]. The open symbols are the data points with statistical and systematic errors added in quadrature, the filled ones are the corresponding results from this analysis.



Figure 4: The calculated ratio $R_{F_2}^A(x, Q^2)$ compared with the NMC 95 (squares) [27] and the reanalysed NMC 95 (circles) data [26].



Figure 5: The computed ratio $R_{F_2}^A(x, Q^2)$ vs. $R_{F_2}^{Li}(x, Q^2)$ (filled circles) compared with the NMC data [26] (open circles).



Figure 6: The calculated ratio $R_{F_2}^{Cu}(x, Q^2)$ (filled squares) compared with the EMC [31] data (open squares).



Figure 7: The calculated ratios $R_{F_2}^A(x, Q^2)$ (filled squares) for several nuclei compared with the SLAC data [25] (open squares).



Figure 8: The calculated scale evolution (solid black lines) of the ratio $F_2^{\text{Sn}}/F_2^{\text{C}}$ compared with the NMC data [32] for several fixed values of x.



Figure 9: The computed $R_{DY}^{A}(x_2, M^2)$ (filled squares) as a function of x_2 compared with the E772 data [29] (open squares).



Figure 10: The computed $R_{DY}^{A}(x_1, M^2)$ (filled squares) as a function of x_1 compared with the E866 data [30] (open squares) at four different bins of invariant mass M^2 .



Figure 11: The computed nuclear modification ratio R_{dAu} at forward rapidities (filled squares) for negatively-charged hadron production, compared with the BRAHMS data [11] (open squares). The error bars are the statistical uncertainties, and the shaded bands indicate the point-to-point systematic errors. The additional overall normalization uncertainty, is 5%, i.e. $\sigma_N^{\text{norm}} = 0.05$ in eq. (2.11). The upper panels show the comparison without the normalization factor f_N . In the lower panels, the data have been multiplied by the optimized value $f_N = 1.02$.



Figure 12: The computed R_{dAu} (filled symbols) at midrapidity ($\eta = 0$) for inclusive pion production compared with the PHENIX [14, 15] and STAR [16] data (open symbols). The error bars are the statistical uncertainties, and the shaded bands indicate the point-to-point systematic errors. The additional overall normalization uncertainties are 10% for the PHENIX data and 17% for the STAR data. The left panels show the comparison without the normalization factor f_N . In the right panels, from top to bottom, the data have been multiplied by the optimized values $f_N = 1.04$, $f_N = 1.07$ and $f_N = 0.90$.

In comparison with our previous work, ref. [3], the Copper and Lithium data in figures 4–6 have now been added into the analysis. In figure 3, we see that shadowing for heavy nuclei (Sn and Pb) has now gotten stronger, and in figure 7 that we now reproduce the largest-x DIS data better than before. The smallest-x panel of figure 8 is one of the key issues in this paper and the obtained Q^2 slopes will be separately commented in section 4 below. Figure 9 shows that for the DY ratios the A systematics at the smallest values of x_2 have been improved: now also the Tungsten data are reproduced well. This improvement is reflected also in the large- x_1 part of the W/Be ratio in figure 10.

The data set that plays a major role in constraining the gluon modifications in the present analysis, is the inclusive negatively-charged hadron production at forward direction $(\eta = 2.2 \text{ and } \eta = 3.2)$ measured by the BRAHMS collaboration at RHIC, shown in figure 11. For the data sample we include in the global fit, $p_T \ge 2 \text{ GeV}$, the optimized normalization factor is close to one, $f_N = 1.02$.

Figure 12 presents the comparison with the PHENIX and STAR measurements of inclusive pion production at midrapidity ($\eta \sim 0$). The need of a treatment which accounts for normalization uncertainties is clearly demonstrated by this figure. Although all data sets agree within the given large uncertainties, the general trend in the STAR data is somewhat different from the PHENIX data, as can be seen in the uncorrected case ($f_N = 1$), shown on the left-hand side of the figure. Taking into account the normalization uncertainties as provided by the modified definition of χ^2 in eqs. (2.11), a good fit with both PHENIX and STAR data sets becomes indeed possible — see the right-hand side of figure 12, where the optimized normalization factors for the PHENIX data are $f_N = 1.04$ and 1.07 and for the STAR data $f_N = 0.90$.

4. Discussion

Figure 13 shows a comparison of the nuclear effects in the average valence quark, average sea quark and gluon distributions at our initial scale $Q_0^2 = 1.69 \,\text{GeV}^2$, as obtained for a Lead nucleus in the LO DGLAP analyses here (EPS08), in HKN07 [7], in nDS [6], and in our previous works EKPS [3] and EKS98 [2]. The figure demonstrates the fact that while the average effects in the valence quarks and in the mid-x region $(0.01 \leq x \leq 0.2)$ of the sea quarks are relatively well under control, quite large uncertainties remain in the large-x ($x \geq 0.2$) sea quark and gluon distributions. In particular, the gluon shadowing which we obtain here on the basis of the BRAHMS data, is clearly stronger than in the previous global analyses. A strong gluon shadowing has been suggested before at least in the Glauber-Gribov framework [35, 36] (see also the review [37]) and also in the context of DGLAP evolution [38], but not in a global DGLAP analysis where constraints from DIS, DY and RHIC hadron production data are simultaneously imposed.

The obtained gluon shadowing reflects a compromise between a weaker gluon shadowing suggested by the NMC 96 DIS data [27] (the first panels in figure 8), and a stronger effect demanded by the BRAHMS data. Regarding these constraints, we note the following:

First, the DIS data [27] show that the Q^2 dependence of R_{F_2} at $x \sim 0.01$ in the region $Q^2 \gtrsim 1 \,\text{GeV}^2$ is very weak. Given this, the small-*x* approximation of the DGLAP



Figure 13: Comparison of the average valence and sea quark, and gluon modifications at $Q^2 = 1.69 \text{ GeV}^2$ for Pb nucleus from LO global DGLAP analyses EKS98 [2], HKN07 [7], nDS [6], EKPS [3] and this work EPS08.



Figure 14: The correlation between the gluon shadowing (left), the Q^2 slopes of $F_2^{\text{Sn}}/F_2^{\text{C}}$ (middle) and the forward- ηR_{dAu} (right) when weights $w_N = 0$, 40 and 150 are assigned for the BRAHMS data. In the right panel, the comparison is shown without an overall normalization factor, i.e. with $f_N = 1$.

equations [39, 40],

$$\frac{\partial R_{F_2}^{\mathrm{A}}(x,Q^2)}{\partial \log Q^2} \approx \frac{10\alpha_s}{27\pi} \frac{xg(2x,Q^2)}{F_2^{\mathrm{D}}(x,Q^2)} \times \left[R_G^{\mathrm{A}}(2x,Q^2) - R_{F_2}^{\mathrm{A}}(x,Q^2) \right], \tag{4.1}$$

then indicates that gluon shadowing is restricted to be similar to what has been measured for F_2 .

Second, using eq. (4.1) above, and the fact that the $\log Q^2$ -slope of $F_2^{\text{Sn}}/F_2^{\text{C}}$ measured by NMC has been observed to be positive at x = 0.125 — see the first panel in figure 8 we deduce that

$$\frac{R_G^{\mathrm{Sn}}(2x,Q^2)}{R_G^{\mathrm{C}}(2x,Q^2)}\Big|_{x\approx 0.0125} > \frac{R_{F_2}^{\mathrm{Sn}}(x,Q^2)}{R_{F_2}^{\mathrm{C}}(x,Q^2)}\Big|_{x\approx 0.0125.}$$
(4.2)

This indicates that the A dependence of gluon shadowing is weaker than that of F_2 .

Third, the A dependence of gluon shadowing must still be strong enough in order to reproduce the BRAHMS data. The flattening of the Q^2 -slope seen in the first panel of figure 8 indicates that the gluon shadowing now obtained — the A dependence of the gluon modifications in particular — is already so strong that it is in the brink of violating the condition (4.2). In this sense the gluon shadowing in the present global fit is the strongest possible one which is still in agreement with the DIS data.

Fourth, a balance between the constraints that the NMC 96 and BRAHMS data offer for the gluon shadowing, is obtained by assigning suitable relative weights, see table 1. Since these data sets drive the fit to opposite directions, the resulting gluon shadowing obviously depends on the weights introduced. To demonstrate this sensitivity, we have repeated the analysis by varying the BRAHMS data weights as follows: By setting $w_N = 0$, we remove this data set from the analysis. Alternatively, by assigning a very large weight, $w_N = 150$, to the BRAHMS data, we clearly overemphasize its importance. In both cases, the smallest-x NMC 96 data set weight is kept unchanged ($w_N = 10$, see table 1). The overall fits obtained in these extreme cases remain very good, giving $\chi^2/N = 0.72$ and 0.73, correspondingly. Figure 14 (left panel) shows the resulting gluon modifications in each case, along with a comparison to the smallest-x NMC 96 data (middle panel) and the BRAHMS data (right panel). The figure clearly demonstrates how adding more weight to the BRAHMS data will eventually flip the sign of the computed Q^2 slopes of $F_2^{\rm Sn}/F_2^{\rm C}$ a phenomenon which on the basis of the systematics seen in the NMC 96 data would be an unwanted feature. With a weight factor $w_N = 40$ for the BRAHMS data (making the effective number of the BRAHMS data points the same as in the three smallest-x panels of the NMC 96 data), we reach the strongest possible gluon shadowing, and thus a fair agreement with the measured forward-rapidity R_{dAu} , without such a sign flip.

Naively, in the RHIC hadron data, we could well expect that hadrons at fixed η and p_T would dominantly come from partons of higher transverse momenta, $q_T \sim 1.5...2p_T$ and the same rapidity η [22], whose production would mainly probe the nPDFs at momentum fractions $x_2 = \frac{q_T}{\sqrt{s}}(e^{-\eta} + e^{-y_2}) \approx \frac{4p_T}{\sqrt{s}}e^{-\eta} \sim 10^{-3}$, assuming $2 \to 2$ parton production kinematics, and taking $p_T \sim 2 \text{ GeV}$ and $y_2 \sim \eta = 3.2$. We notice, however, that the ratio $R_{\rm dAu}$ at $p_T = 2 \,{\rm GeV}$ in figure 11 is considerably larger than the gluon shadowing we obtain at these values of x, see figure 13 (solid line). This is due to two reasons: First, as shown in figure 13 of [3], the DGLAP evolution from Q_0 to the few-GeV region increases the ratio R_G^A substantially. Second, the integration over the partonic q_T and over the unobserved parton rapidity y_2 causes a significant smearing of the x-range probed, especially towards larger x (see also ref. [41] and table 1 in [10]). Thus, the ratio R_{dAu} at forward η is in fact sensitive not only to nuclear gluon shadowing but also to gluon antishadowing — and antishadowing in turn amplifies when shadowing gets stronger. Therefore, even a large change in gluon shadowing induces only a moderate change in the computed ratio $R_{\rm dAu}$, and a significant gluon shadowing is required in order to reproduce the BRAHMS data at $p_T \geq 2 \,\mathrm{GeV}.$

As seen in figures 11 and 12, we have a good fit of the nuclear modification factor R_{dAu} at $p_T \geq 2 \text{ GeV}$. We cannot, however, reduce R_{dAu} by strengthening the gluon shadowing as much as the BRAHMS data below 2 GeV would require without violating the DIS data constraints. This is also one of the reasons for excluding the region $p_T < 2$ GeV of the RHIC data from this analysis. As explained above, we also are hesitant to push the nuclear case too far into the small- p_T region, for we cannot reproduce the shape of the absolute p_T spectra in p+p collisions well enough there, and for we do not consider impact-parameter dependence of nPDFs or a more detailed centrality selection here.

As illustrated by figure 13, a saturation of shadowing at $x \to 0$ was assumed in previous global analyses. This assumption is now relaxed with the aim to study the strongest gluon shadowing allowed by present experimental data. It is worth emphasizing that the behavior of the nuclear corrections at the smallest values of x ($x \leq 10^{-3}$) is still largely determined by the assumed shape of the fit functions in eq. (2.3). This limitation is common to any global fit (for nPDFs as well as for the free proton PDFs) in those regions of phase space which are poorly or not at all constrained by the data.

5. Conclusions

We have improved the global analysis of nPDFs in two important ways: First, by taking the RHIC data into account in such analysis for the first time, we have extended the constrained x region down to $x \gtrsim 10^{-3}$. Second, we have improved the χ^2 minimization procedure by introducing weighting of different data sets and by explicitly accounting for the overall normalization errors quoted by the experiments.

One of the main goals of this paper is to study to what extent a strong gluon shadowing suggested by the BRAHMS data can be accommodated together with the DIS and DY data in a global analysis. We conclude that a simultaneous fit of DIS, DY and high- p_T ($p_T \geq 2 \,\text{GeV}$) hadron production data from RHIC at forward rapidities (BRAHMS negative hadrons), is indeed possible within the DGLAP framework without invoking any new suppression mechanism. Thanks to the improved treatment of data normalization errors, we obtain also a good agreement with the RHIC pion data at mid-rapidity (STAR and PHENIX). The very good quality of the global fit obtained suggests that a well-working universal set of nPDFs can be extracted in the framework of collinear factorization. Within an improved global χ^2 analysis, and with an emphasis on the RHIC forward-rapidity data, we obtain a stronger gluon shadowing than in the previous global nPDF analyses, see figure 13. These are the main new results of this paper. The LO nPDF set we have obtained (EPS08), i.e. a parametrization of the x, Q^2 and A-dependent nuclear modifications relative to CTEQ6L1, is available at [17] for practical use.

As discussed above, the amount of gluon shadowing obtained depends on the weight assigned to the BRAHMS data, and equally good overall fits can be obtained also when the weights are smaller and the resulting gluon shadowing is weaker. Until more data become available to resolve this problem, the nuclear gluon distributions suffer from considerable uncertainties. To estimate the effects of these uncertainties in the hard process cross sections one computes in LO, we recommend to use the current results, EPS08, in parallel with the previous LO results EKS98 [2], nDS [6] and HKN07 [7]. Regarding inclusive hadron production in nuclear and hadronic collisions, computed here in the collinear factorization framework, we would like to emphasize that we have limited the study to the region $p_T \geq 2 \text{ GeV}$: Within the present global analysis, we cannot reproduce the sudden drop of the ratio R_{dAu} measured for negative hadrons by BRAHMS at $p_T < 2 \text{ GeV}$ at forward rapidities, see figure 11, or the very strong suppression of R_{dAu} measured by STAR for π^0 at $\eta = 4$ and $p_T < 2 \text{ GeV}$ [42] — a yet stronger gluon shadowing needed for this would clearly lead into a contradiction with the log Q^2 slopes of $F_2^{\text{Sn}}/F_2^{\text{C}}$ measured at DIS. More detailed work on fragmentation functions, impact parameter dependence of the nPDFs as well as further developments in the fit functions is required in order to make firmer conclusions on the applicability of the DGLAP-evolved universal nPDFs in this region. Regarding the fragmentation functions, we anticipate that considering a more detailed charged separation (see e.g. [43-45]) in hadron production would tend to increase the computed R_{dAu} rather than decrease it. Such further complication in extracting the gluon shadowing from the BRAHMS data is, however, not considered here, since the inclusion of the charge separation becomes more reliable only in NLO.

Our next goal is to perform this analysis in NLO, as well as, when the data become finalized, include other RHIC data sets, such as photon production in d+Au and Au+Au from PHENIX, into the analysis. In general, any further constraints for the gluon distributions are more than welcome. For example, the ratio R_{dAu} for D mesons to be (hopefully soon) measured at RHIC will be extremely useful, at any rapidity. The cleanest environment for the nPDFs measurements would be in the DIS experiments at eRHIC [46] and LHeC colliders now being discussed. Before the possible realization of these machines, we hope that the present study in its part demonstrates how important it would be for the correct determination of universal nPDFs to have a systematic proton-nucleus program also at the LHC: further constraints for nuclear gluons in the yet unexplored regions of the x, Q^2 plane are absolutely necessary for understanding QCD parton dynamics in high-energy nuclear and hadronic collisions.

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